
Application of bi-spectral techniques to Virgo Data

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Summary

- When & Why ?
- What is the Bicoherence ?
- The Bicoherence Tool
- The Virgo Data Set
- The Virgo Bicoherence
- Next Steps

When & Why

- **When** : non Gaussian noise, non-linear response... , non stationary noise...
- **Why** : because of bilinear couplings of noise sources / signal disturbances.
- Consider a physical process, which puts out the value of the product of two signals at two different frequencies

$$s_1 = a_1 \sin(2\pi f_1 t + \phi_1) \quad s_2 = a_2 \sin(2\pi f_2 t + \phi_2)$$

- The output signal will then be

$$S = s_1 + s_2 + k s_1 s_2$$

- where **k** is a coupling factor which in general could be frequency dependent. As we can expect, there will be two additional frequencies at

$$f_1 - f_2, f_1 + f_2$$

What is the bicoherence ?

- The bicoherence is a normalized form of the bispectrum :

$$S_{3x}(f_1, f_2) = \langle \tilde{X}(f_1) \tilde{X}(f_2) \tilde{X}^*(f_1 + f_2) \rangle$$

- and is defined as

$$b(f_1, f_2) = \frac{S_{3x}(f_1, f_2)}{\sqrt{S_{xx}(f_1)S_{xx}(f_2)S_{xx}(f_1 + f_2)}}$$

- where X_k , X_l and X_m are the Fourier components of the signal at the frequencies k , l and $m=l+k$, If the signal at $m=l+k$ arises due to the product of the signal at k and l , then for the phase of the numerator

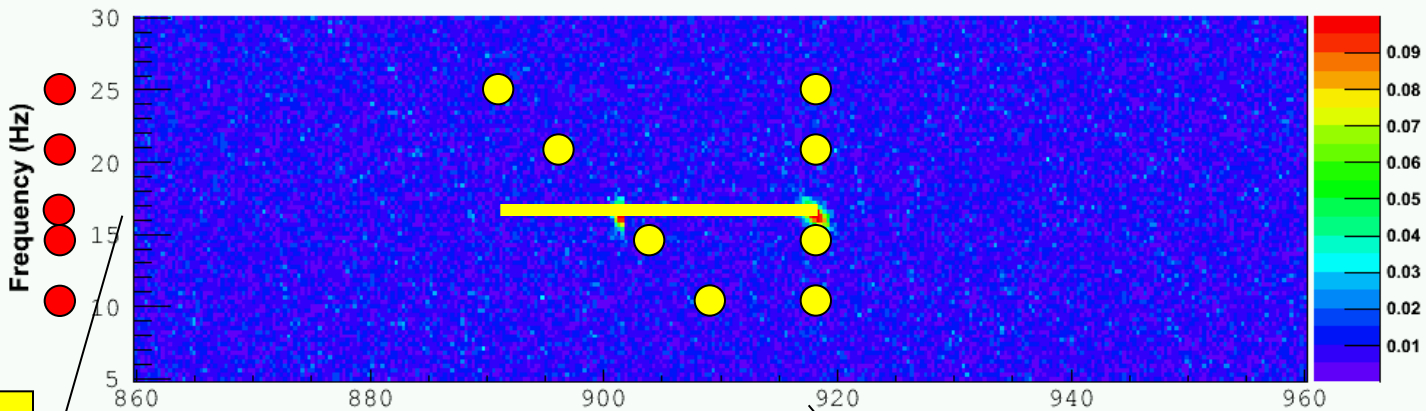
$$e^{i\phi_1} e^{i\phi_2} e^{-i(\phi_1 + \phi_2)}$$

will average out to a nonzero value and hence the bispectrum will be nonzero

Example

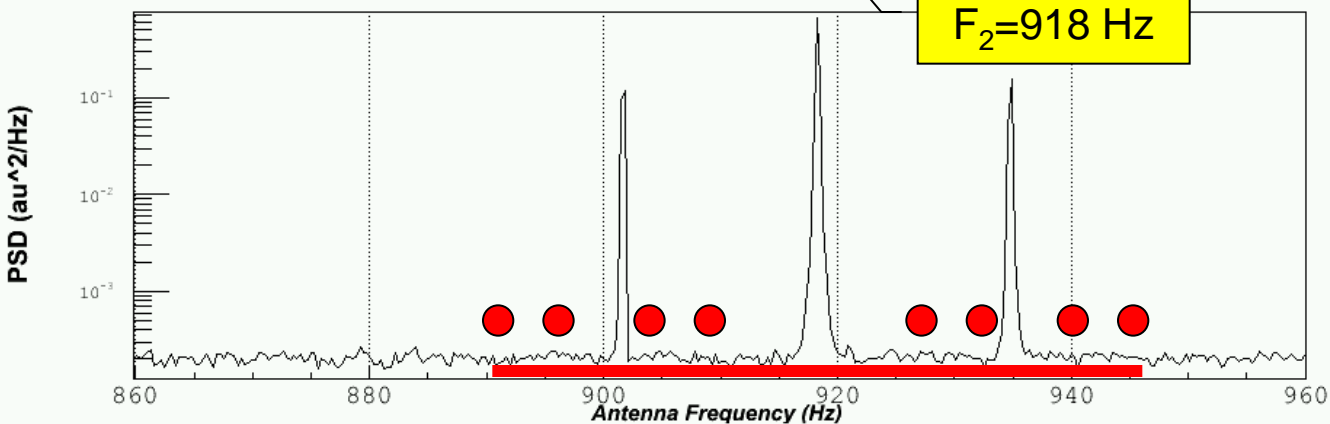
$$F_1=16.5 \text{ Hz}, F_2=918 \text{ Hz}$$

$$F_2-F_1=901.5 \text{ Hz}, F_2+F_1=934.5 \text{ Hz}$$



$F_1=16.5 \text{ Hz}$

$F_2=918 \text{ Hz}$



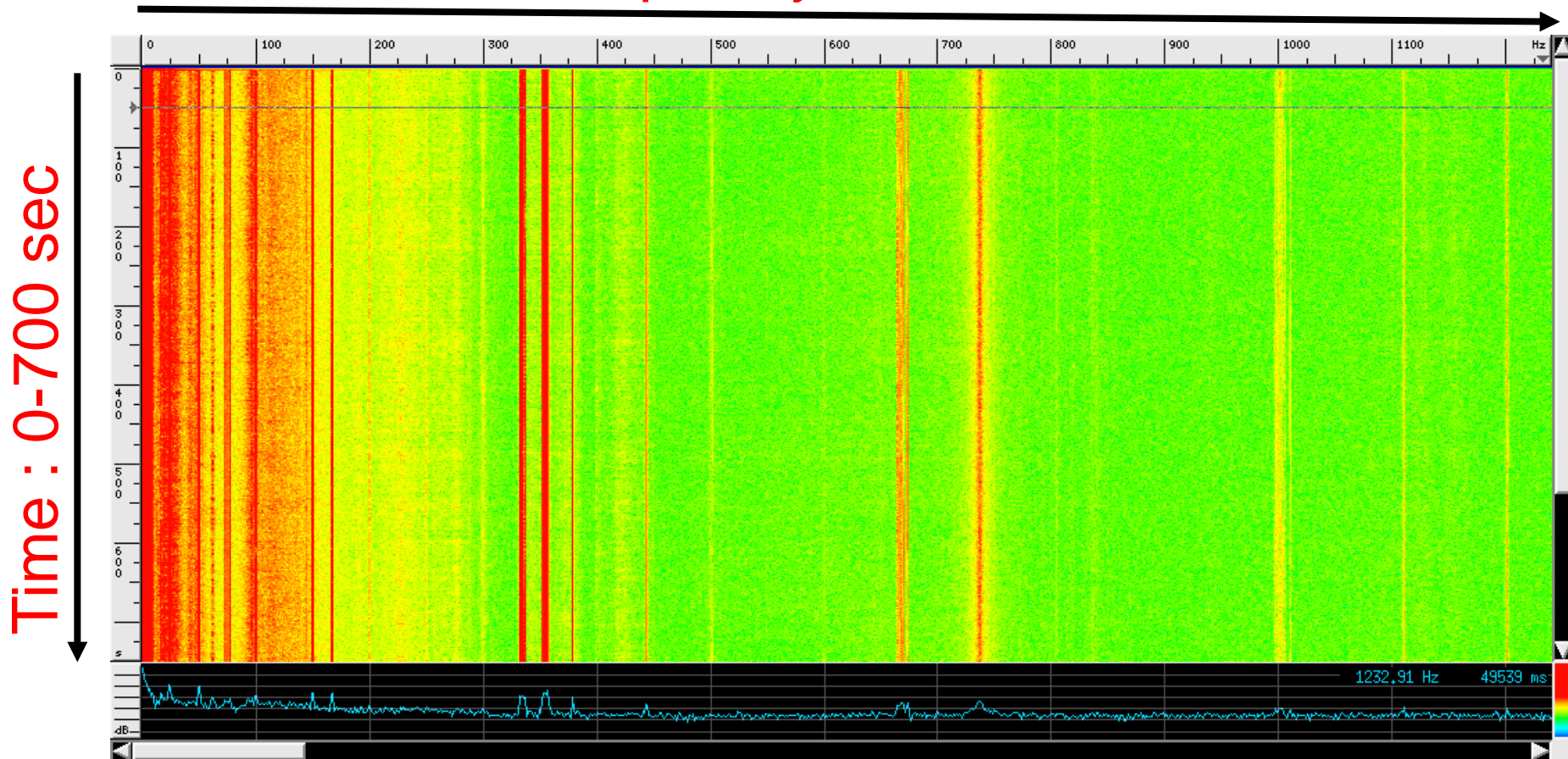
The Bicoherence Tool

- Our bicoherence tool is embedded in the AURIGA Data Analysis, which works in the ROOT framework, reads frame format data files, includes some LAL libraries...
- It has been extremely useful in AURIGA to identify the “bad” low frequency resonances to design the additional suspension stage
- The analysis reported in this talk has been implemented with a ROOT macro
- Performances : Intel Xeon CPU 3.4GHz
 - Sample Rate : 20KHz
 - Analyzed Frequency Area : 5Hz x 50Hz
 - Frequency Resolution : 0.03125 Hz
 - # average : 250
 - Speed : 44x (8000 sec of data analyzed in 186 sec)

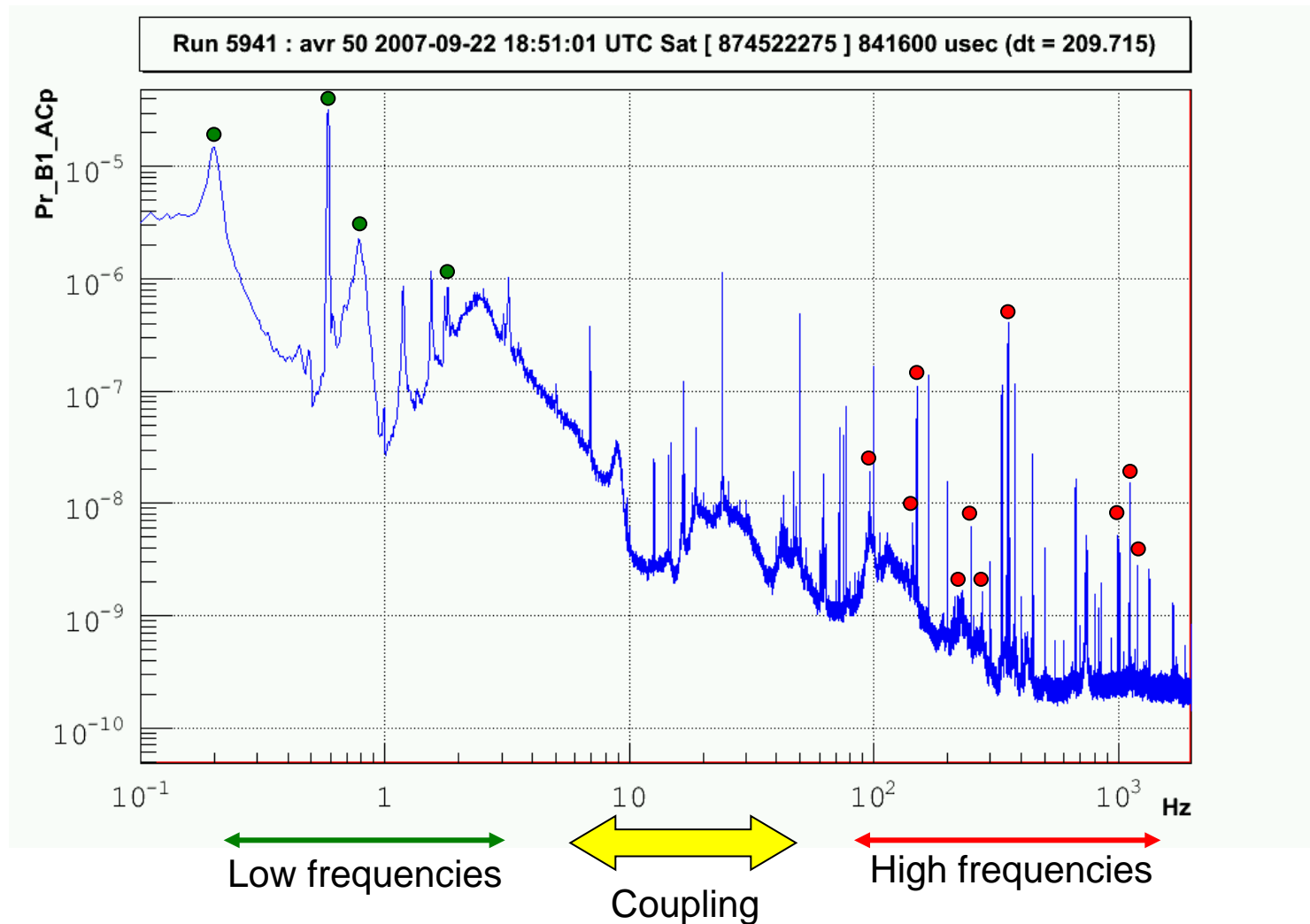
Virgo Data Set

Run 5941 : Channel : V1:Pr_B1_ACp : 2007-09-22 17:00:00

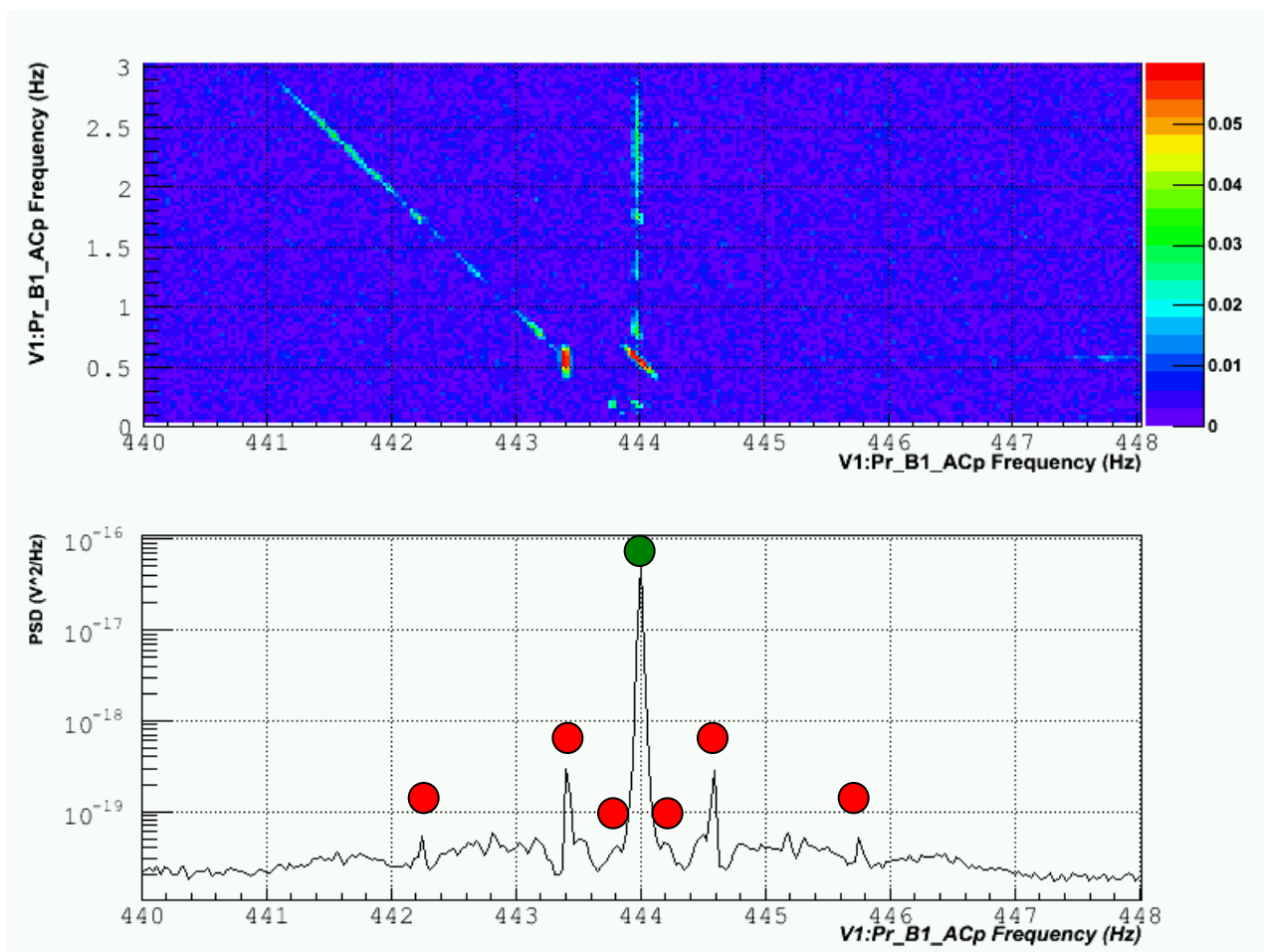
Frequency : 0-1250 Hz



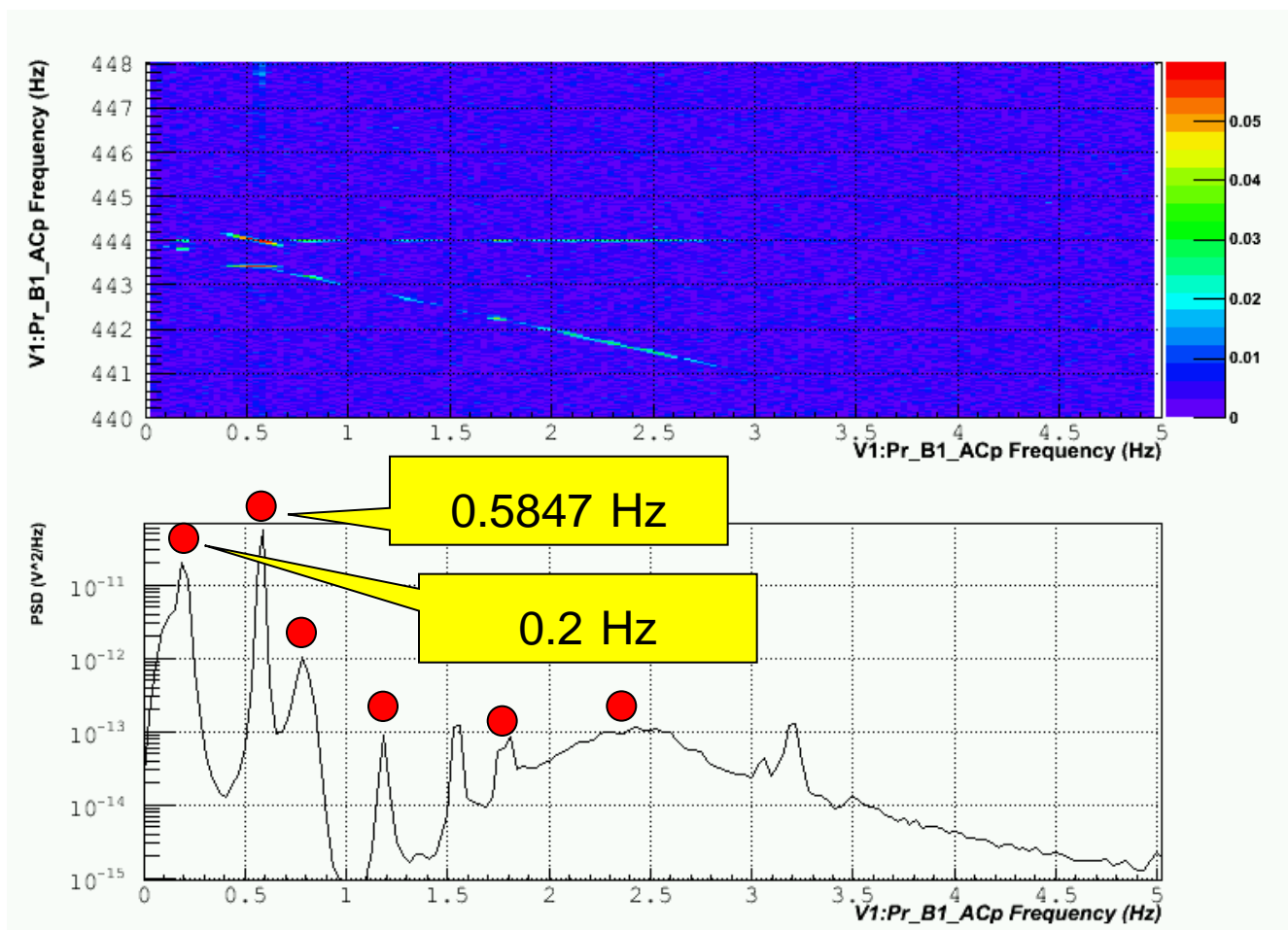
Bilinear Coupling in Virgo



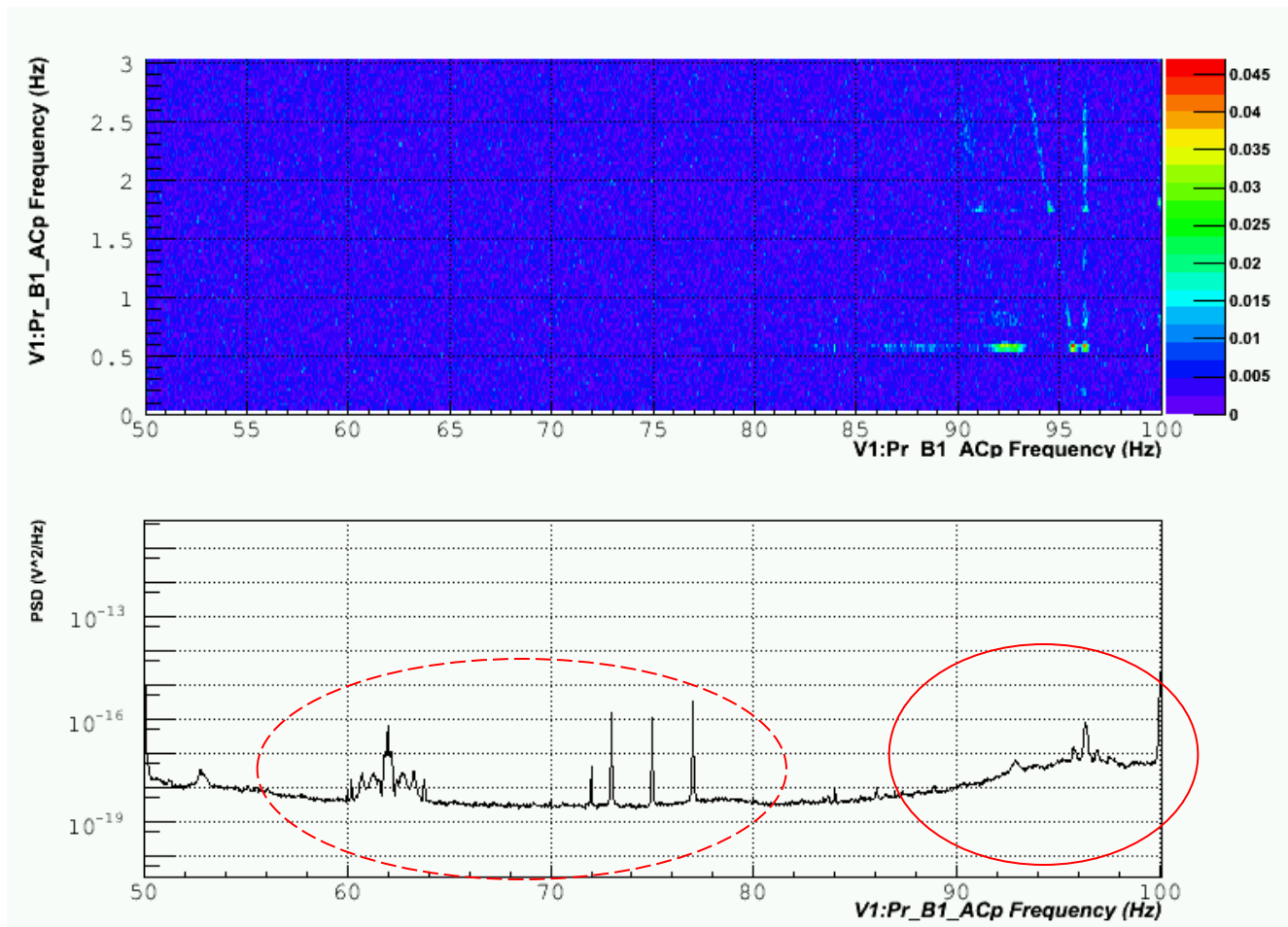
Bicoherence @ 444 Hz



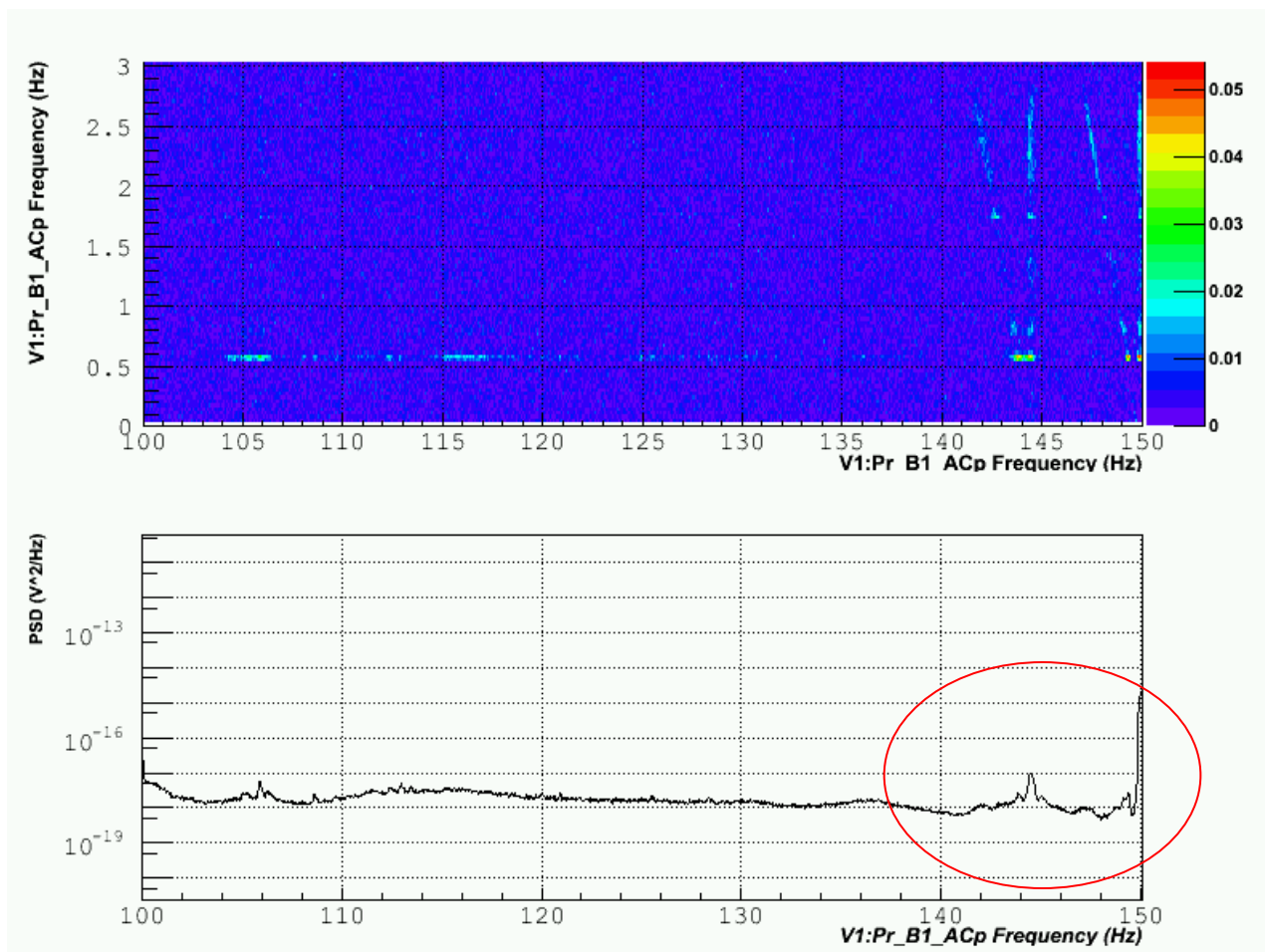
Bicoherence @ 444 Hz



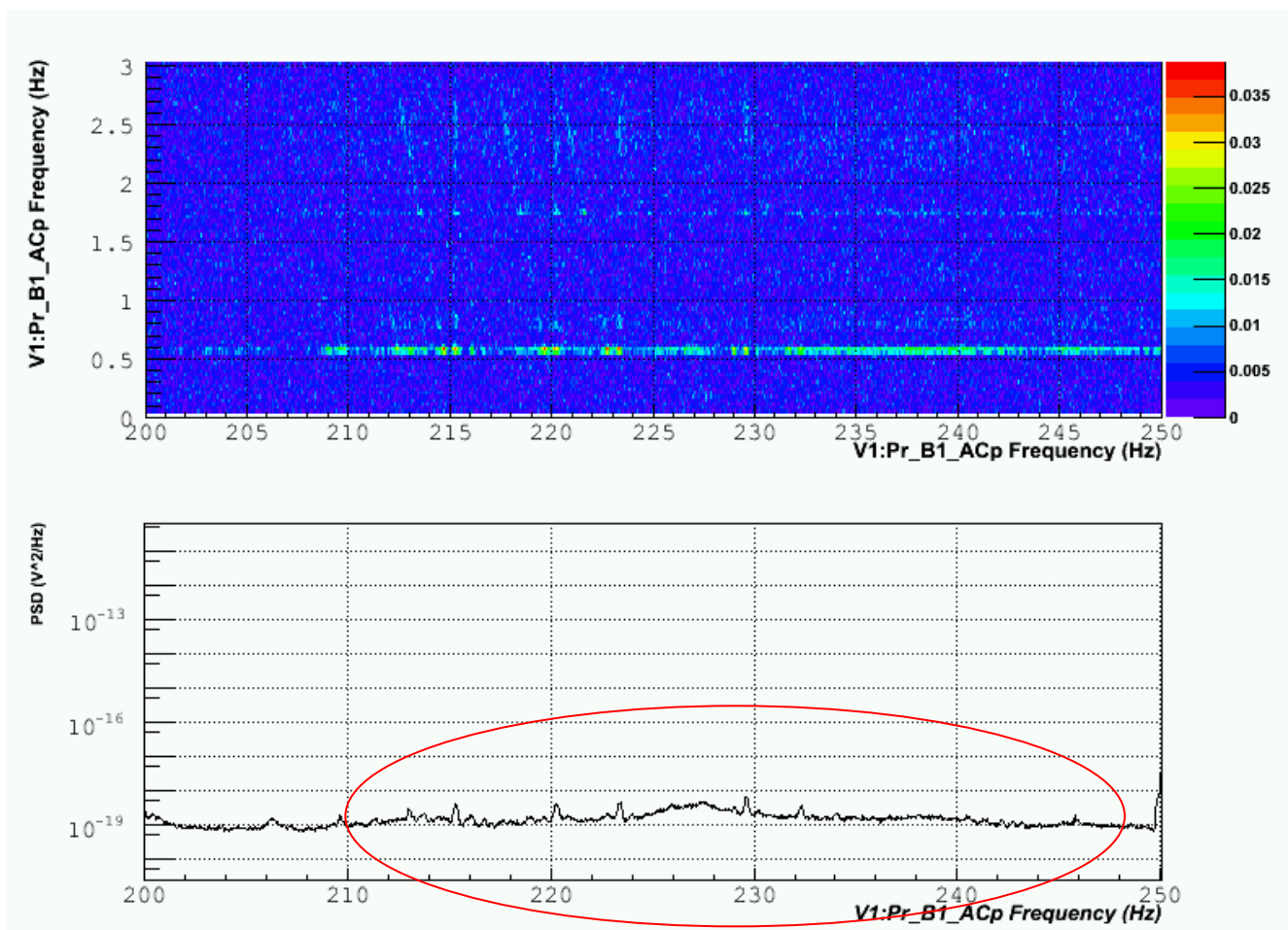
Bicoherence @ 50-100 Hz x 0-3 Hz



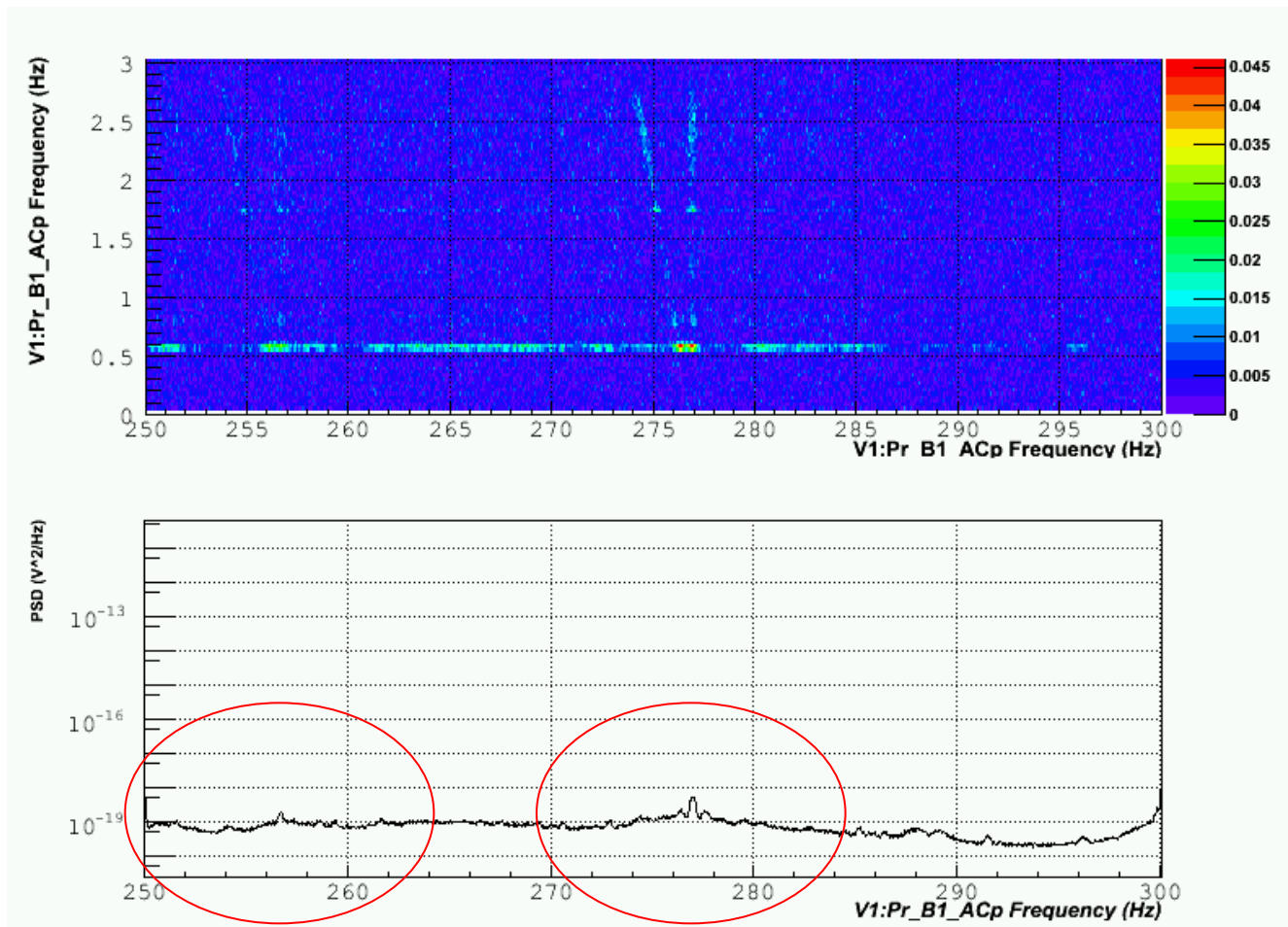
Bicoherence @ 100-150 Hz x 0-3 Hz



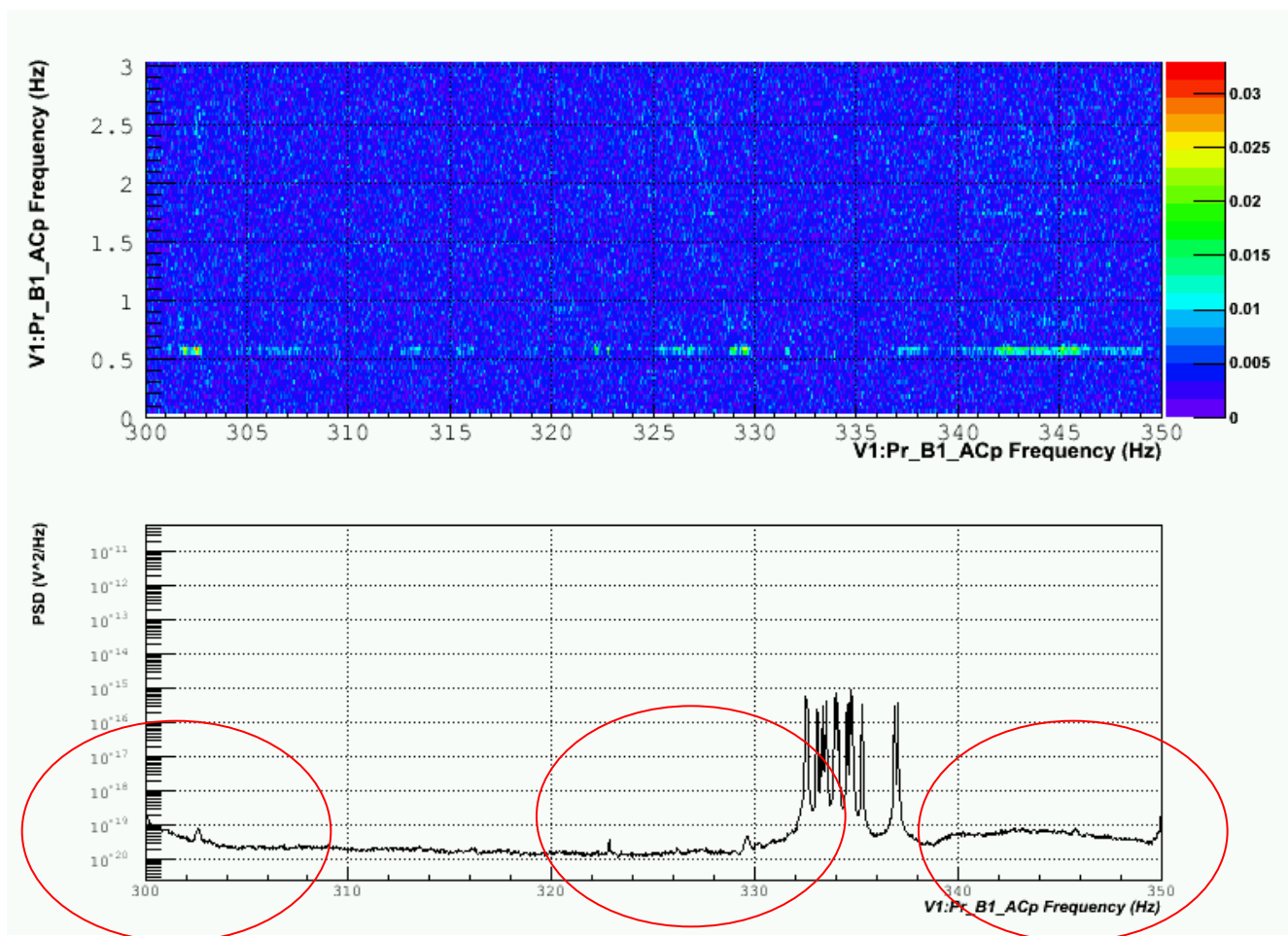
Bicoherence @ 200-250 Hz x 0-3 Hz



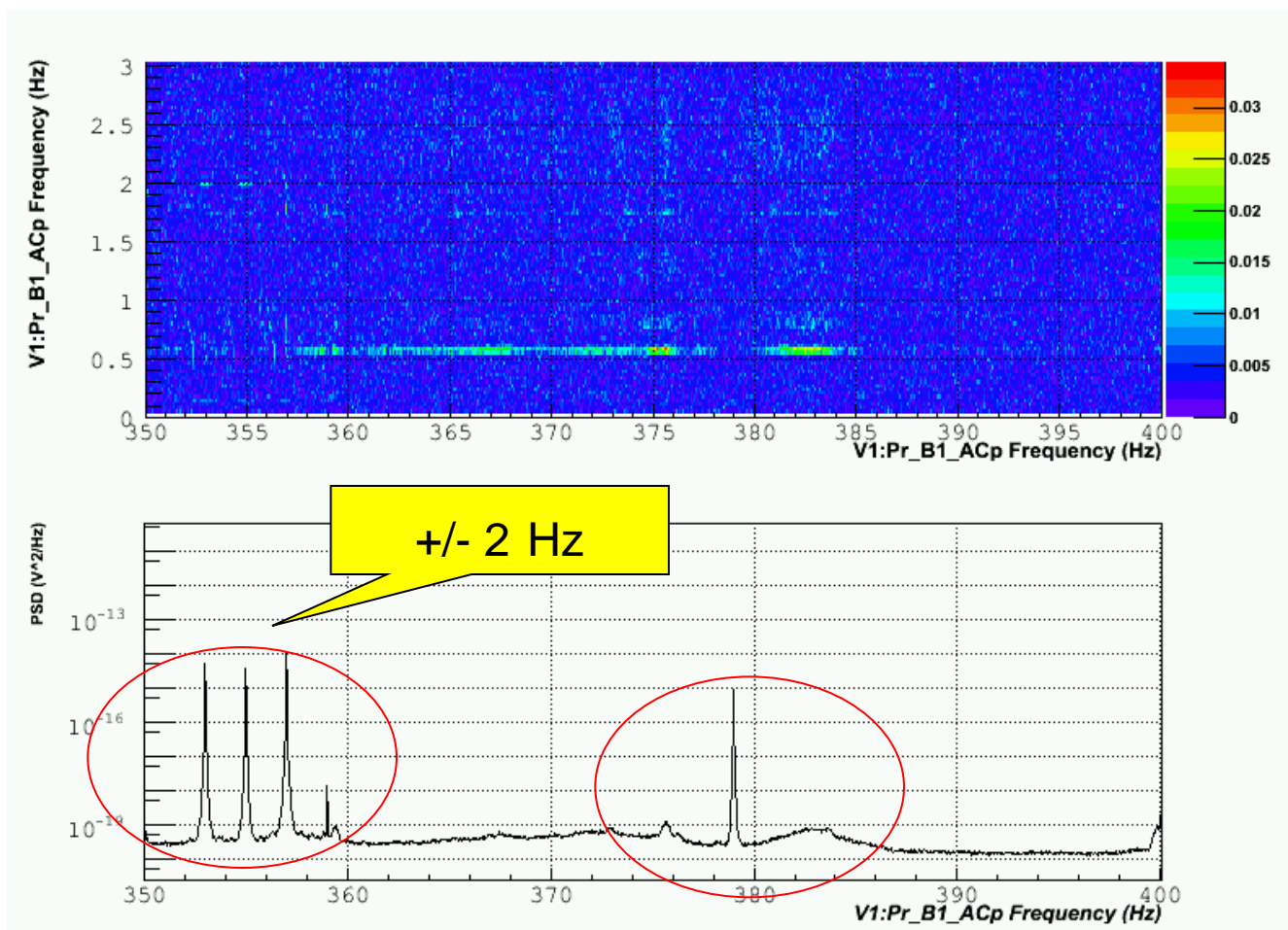
Bicoherence @ 250-300 Hz x 0-3 Hz



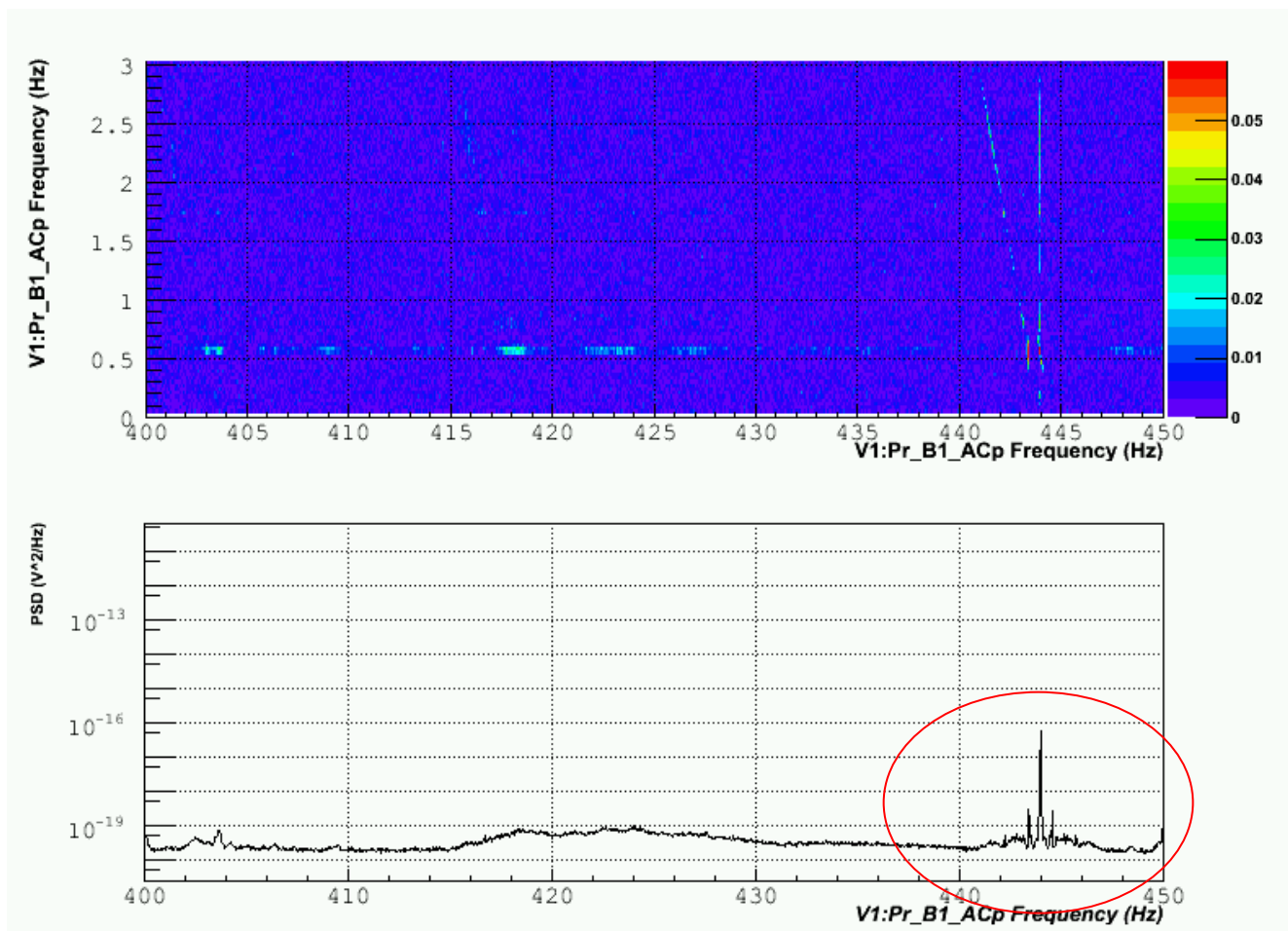
Bicoherence @ 300-350 Hz x 0-3 Hz



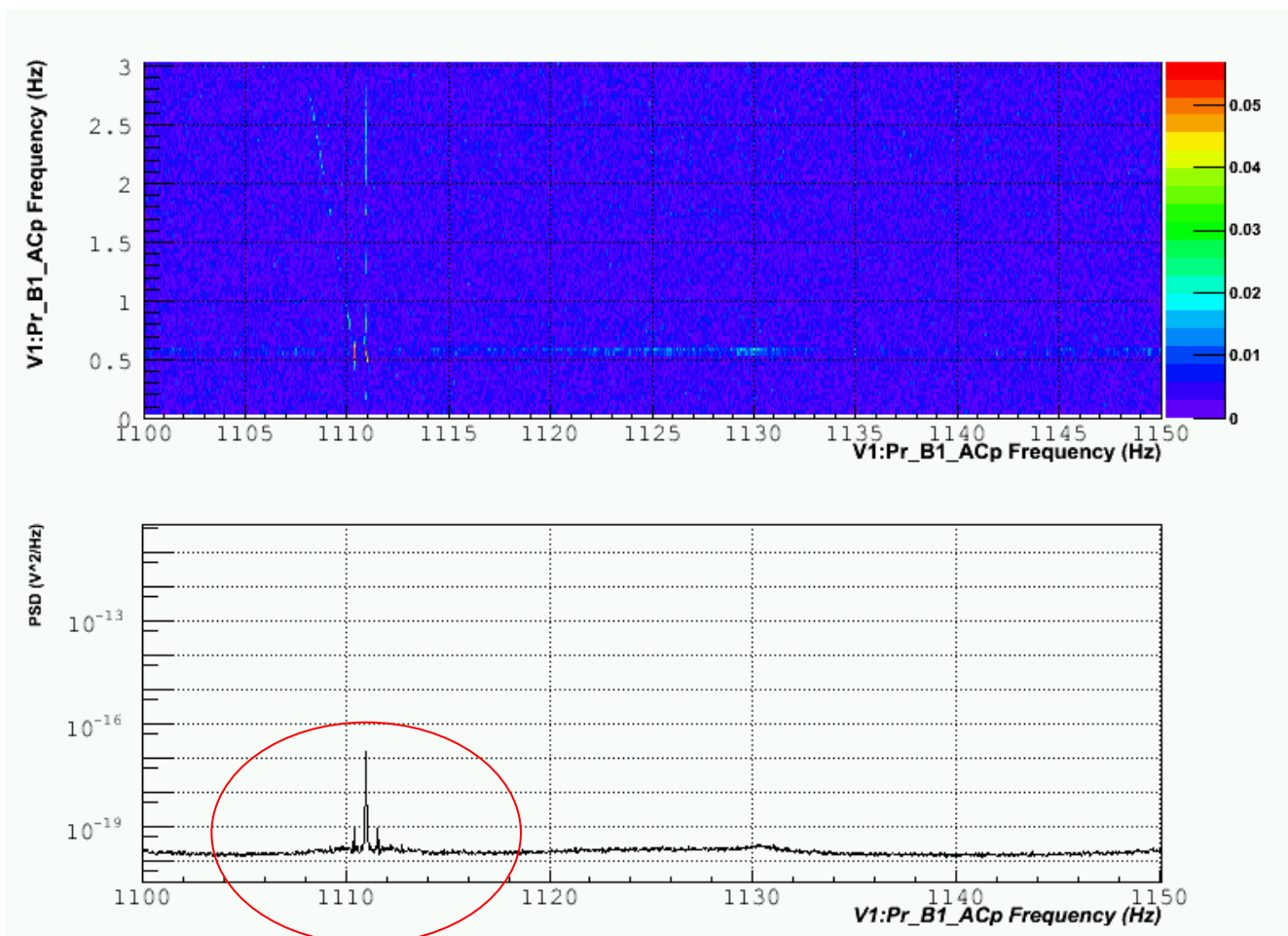
Bicoherence @ 350-400 Hz x 0-3 Hz



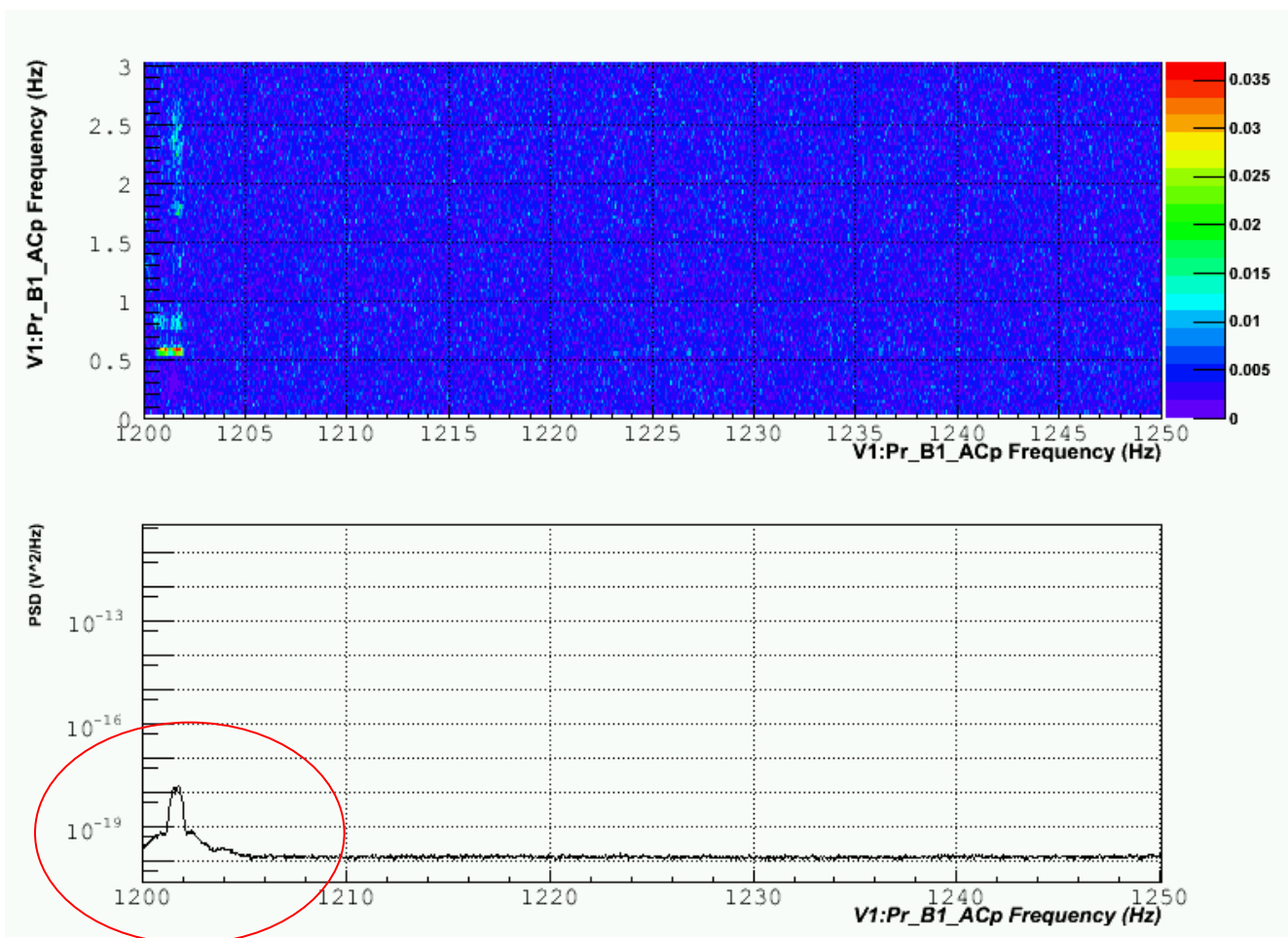
Bicoherence @ 400-450 Hz x 0-3 Hz



Bicoherence @ 1000-1150 Hz x 0-3 Hz



Bicoherence @ 1200-1250 Hz x 0-3 Hz



Next Steps

- Feedback from HW Virgo peoples
- Analysis of data set with different setup
 - Comparisons could highlight the origin of the non linearities
- Implementation of an offline tool under ROOT framework (? if useful)